

# Thermal Matter

## Thermal Expansion

### Linear Expansion

$$\alpha = \frac{\Delta l}{l \Delta T}$$

$\alpha$  = coefficient of linear expansion  
 $\Delta l$  = change in length  
 $\Delta T$  = rise in temp

### Areal Expansion

$$\beta = \frac{\Delta A}{A \Delta T}$$

$\beta$  = coefficient of areal expansion  
 $\Delta A$  = change in length

### Volume Expansion

$$\gamma = \frac{\Delta V}{V \Delta T}$$

$\gamma$  = coefficient of volume expansion  
 $\Delta V$  = change in volume

### Relation between $\alpha$ , $\beta$ and $\gamma$

$$\alpha = \frac{\beta}{2} = \frac{\gamma}{3}$$

### Measurement of Temperature

$$\frac{C}{100} = \frac{F - 32}{180} = \frac{K - 273}{80}$$

### Construction of Thermometer

If length of mercury column at  $0^\circ$  and  $100^\circ$  are  $l_0$  and  $l_{100}$  respectively and at  $t^\circ$  the length of mercury is  $l_t$ .

$$\frac{l_t - l_0}{t} = \frac{l_{100} - l_0}{100}$$

### Resistance Thermometer

If  $R_0$ ,  $R_{100}$  and  $R_t$  are the resistances of a platinum wire at temperature  $0^\circ\text{C}$ ,  $100^\circ\text{C}$  and unknown temperature ( $t^\circ\text{C}$ )

$$\frac{R_t - R_0}{t} = \frac{l_{100} - l_0}{100}$$



**Specific Heat Capacity (S)**  
Heat capacity per gram of substance

$Q = m S \Delta T$   
 $m$  = mass of substance  
 $Q$  = Heat Required  
 $\Delta T$  = Change in temperature

**Specific Heat capacity of water = 4.184 J/g or 1 cal/g**

**Molar Specific Heat Capacity**

$$c = \frac{\Delta Q}{\mu \Delta T}$$

$\mu$  = No. of moles of substance

**Latent Heat**

$m$  = mass of substance  
 $L$  = Latent Heat of Substance  
 $Q$  = Heat required

$$Q = m L$$

**Principle of Calorimetry**

When a hot body is mixed with cold body, then heat lost by hot body is equal to the heat gained by cold body.

$$T_{mix} = \frac{m_1 c_1 T_1 + m_2 c_2 T_2}{m_1 c_1 + m_2 c_2}$$

## Transmission of Heat

**Thermal Conductivity**

$K$  = coefficient of thermal conductivity

$A$  = area of cross-section

$l$  = length of rod

$t$  = time

$\Delta \theta$  = temperature difference between the end of the rod

$$Q = \frac{KA\Delta\theta t}{l}$$

## Thermal Resistance

$$R = \frac{l}{KA}$$

## Newton's Law of Cooling

The rate of loss of liquid is directly proportional to the difference in Temp. of the liquid and its surroundings.

$$-\frac{dT}{dt} \propto (T - T_0)$$

## Radiations

$$\lambda_m T = \text{constant (b)}$$

### Wein's Displacement Law

Wavelength corresponding to maximum emission decreases with increasing temperature

$\lambda_m$  = wavelength corresponding to which max energy is radiated

T = Absolute temperature

b = Wein's constant  
 $= 2.898 \times 10^{-3}$  mK

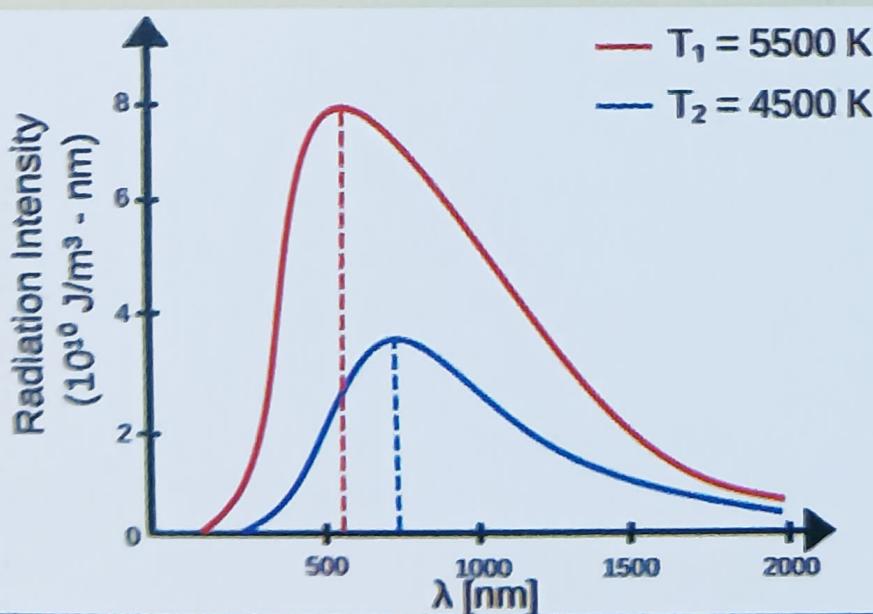
### Stefan's Law

$$\sigma = \text{Stefan's constant} \\ = 5.735 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$$

$$E \propto T^4 \\ E = \sigma T^4$$

Energy radiated by whole body in t time

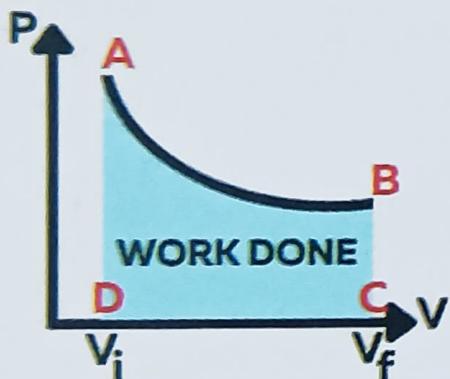
$$E = \sigma A t T^4$$



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# Thermodynamics

## Work done by a thermodynamic system



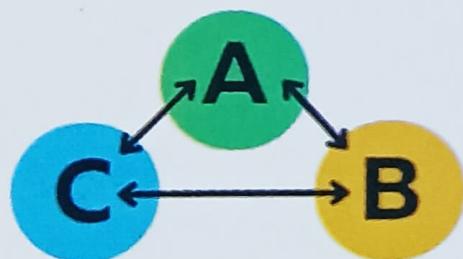
$$W = p \times \Delta V$$

Work done in process A-B

$$W = \int_{V_i}^{V_f} p \Delta V = \text{Area } ABCDA$$

## Zeroth Law of Thermodynamics

According to this law, two systems in thermal equilibrium with a third system separately, are also in thermal equilibrium with each other.



## First Law of Thermodynamics

Heat given to a thermodynamic system ( $\Delta Q$ ) is partially utilised in doing work ( $\Delta W$ ) against the surrounding and the remaining part increases the internal energy ( $\Delta U$ ) of the system.

$$Q = \Delta U + \Delta W$$

## Second Law of Thermodynamics

It is impossible to transfer heat from a lower temperature body to a higher temperature body without use of an external agency.



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## Entropy (Randomness)

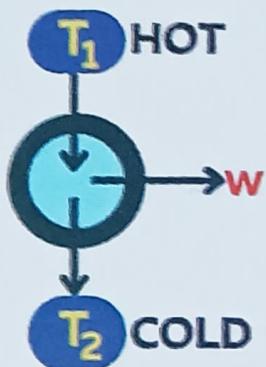
$$dS = \frac{dQ_{rev}}{T}$$

### Entropy

At Constant Temp and Pressure  
or During a Phase Change  
 $L$  = Latent heat

$$dS = \frac{dQ_p}{T} = \frac{dH}{T} = \frac{mL}{T}$$

## Heat engine



Thermal efficiency of a heat engine is given by

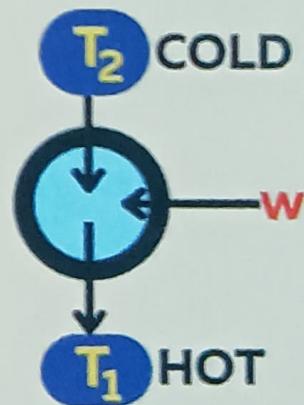
$$\eta = \frac{\text{Work done}}{\text{Total amount of heat absorbed}}$$

$$\eta = 1 - \frac{Q_2}{Q_1} = 1 - \frac{T_2}{T_1}$$

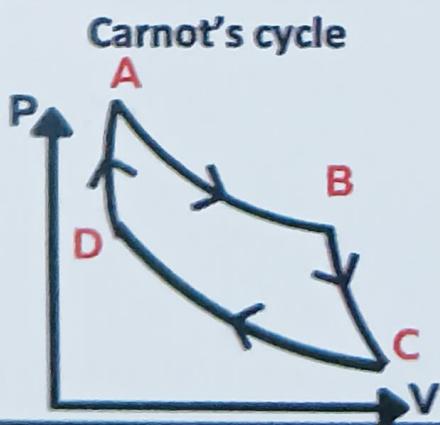
## Refrigerator

$$\beta = \frac{Q_2}{W} = \frac{Q_2}{Q_1 - Q_2} = \frac{T_2}{T_1 - T_2}$$

$$\beta = \frac{1 - \eta}{\eta}$$



### Carnot's cycle



$$\frac{Q_2}{Q_1} = \frac{T_2}{T_1}$$

Efficiency,  
 $\eta = 1 - \frac{T_2}{T_1}$

### Expansions

**AB** : Isothermal

**BC** : Adiabatic

### Compressions

**CD** : Isothermal

**DA** : Adiabatic

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## NEET 2023 PYQ'S (Chapter 9-11)

- The amount of energy required to form a soap bubble of radius 2 cm from a soap solution is nearly:  $3.01 \times 10^{-4}$  J
- The venturi-meter works on : **Bernoulli's Principle**
- Let a wire be suspended from the ceiling (rigid support) and stretched by a weight  $W$  attached at its free end. The longitudinal stress at any point of cross-sectional area  $A$  of the wire is :  $W/A$
- A Carnot engine has an efficiency of 50% when its source is at a temperature  $327^\circ\text{C}$ . The temp. of the sink is  $27^\circ\text{C}$



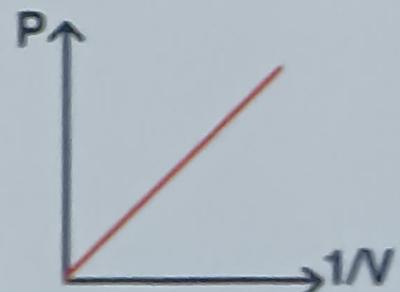
# Gaseous State

Boyle's law

$$P \propto \frac{1}{V}$$

$$P_1 V_1 = P_2 V_2$$

Graphs

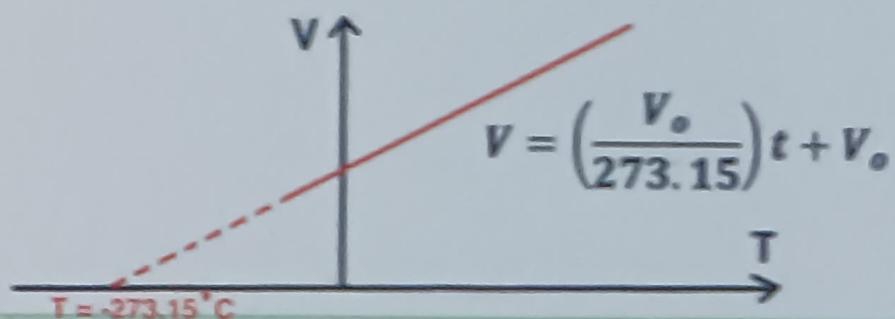


Charles law

$$V \propto T$$

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

Graphs

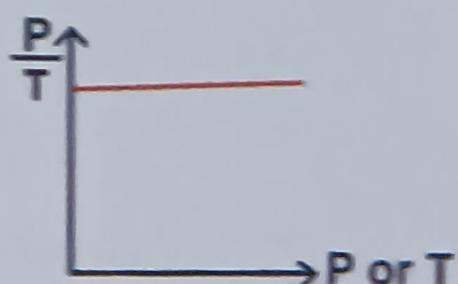
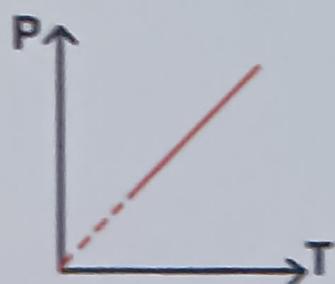


Gay Lussac's Law

$$P \propto T$$

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

Graphs

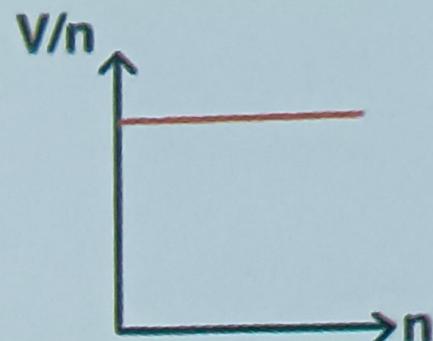
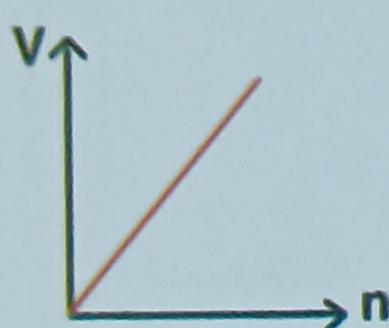


## Avogadro's Law

$$V \propto n$$

$$\frac{V_1}{n_1} = \frac{V_2}{n_2}$$

### Graphs



## Ideal Gas Equation

**Ideal Gas equation**

$$PV = nRT$$

**Combined Gas Law**

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

**Density relation**

$$\rho M = dRT$$

## Dalton's Law of Partial pressure

**For a mixture of a gases**

$$P_{Total} = p_1 + p_2 + p_3 + \dots$$

*p = partial pressures*

**Relation between p & Mole Fraction**

$$p = x \times P_{Total}$$

## Graham's Law of Diffusion

**At Constant T & P**

*if, r = Rate of Diffusion of a gas*

*d = Density of gas*

*M = Molecular Mass*

$$\frac{r_1}{r_2} = \sqrt{\frac{d_2}{d_1}} = \sqrt{\frac{M_2}{M_1}}$$

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